

#39

$$f(x) = \begin{cases} 3-x, & x < 1 \\ ax^2 + bx, & x \geq 1 \end{cases} \quad \begin{array}{l} 3-1 = 2 \\ a(1)^2 + b(1) = 2 \end{array}$$

$$\textcircled{a} \quad a+b=2$$

$$\textcircled{b} \quad f'(x) = \lim_{h \rightarrow 0} \left(\frac{3-(x+h) - (3-x)}{h} \right) = \frac{\cancel{3-x} - h - \cancel{3+x}}{h} = -\frac{h}{h} = -1$$

$$f'(x) = \lim_{h \rightarrow 0} \left(\frac{a(x+h)^2 + b(x+h) - (ax^2 + bx)}{h} \right)$$

$$\lim_{h \rightarrow 0} \left(\frac{\cancel{ax^2} + 2axh + \cancel{ah^2} + \cancel{bx} + bh - \cancel{ax^2} - \cancel{bx}}{h} \right)$$

$$\lim_{h \rightarrow 0} (2ax + ah + b) = 2ax + b$$

$$f'(x) \text{ when } x < 1 \Rightarrow -1$$

$$f'(x) \text{ when } x \geq 1 \Rightarrow 2ax + b \Rightarrow 2a(1) + b = 2a + b$$

slope at
1, $x \geq 1$

$$-1 = 2a + b$$

$$\begin{array}{l} a+b=2 \\ a=2-b \end{array}$$

$$-1 = 2(2-b) + b$$

$$-1 = 4 - 2b + b$$

$$-1 = 4 - b$$

$$\textcircled{b=5}$$

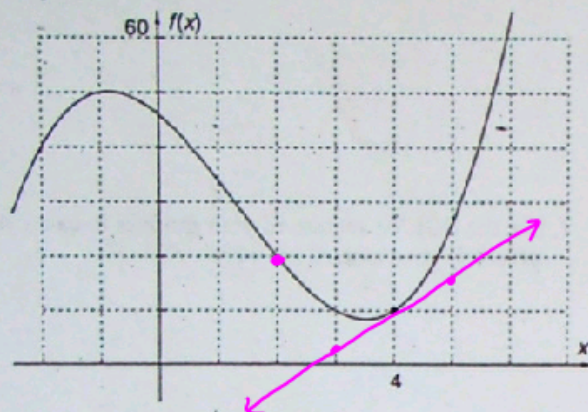
$$a+b=2$$

$$\textcircled{a=-3}$$

The figure shows the graph of

$$f(x) = x^3 - 4x^2 - 9x + 46.$$

In this exercise you will use the definition of derivative to find the *exact* value of $f'(4)$.



1. Find $f(4)$. Show that your answer agrees with the graph.

2. Write the definition of derivative as it applies to f at $x = 4$.

3. Substitute the values of $f(x)$ and $f(4)$ into the definition in Problem 2. Then simplify the resulting rational expression, and take the limit.

4. Plot a line on the graph at $(4, f(4))$ that has slope $f'(4)$. Observe the different scales on the two axes. Tell how the line confirms that the derivative is correct.

$$m = 7$$

$$(4, 10)$$

$$y = 7(x - 4) + 10$$

5. Find the exact value of $f'(2)$ using the same procedure you used for $f'(4)$. How can you tell quickly that your answer is reasonable?

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$f'(4) = 7$$

$$f(x) = 3x^2 - 8x - 9$$

$$f'(2) = 3(2)^2 - 8(2) - 9$$

$$f'(2) = -13$$

5. Plot the numerical derivative, $d'(t)$, as y_2 . Have your instructor check your graph. _____
6. What is true about the graph of d at the point where $d'(t) = 0$? What is happening to the door's motion at this time?
7. Use the SOLVE feature of your grapher to calculate precisely the value of t at which $d'(t) = 0$.
8. Use the MINIMUM feature of your grapher to find precisely the value of t at which $d'(t)$ is a minimum. What does $d(t)$ equal at this value of t ? Put a dot at this point on the graph on this sheet.
9. The point in Problem 8 is called a **point of inflection**. Why do you suppose this name is used?

be smart
Sect. 3.1 #6, 12, 24, 27, 29, 31, 44

3.2 #3, Graph the derivative of #5-10